

Andrew J. Spieker, PhD
BIOS 6312 - Modern Regression Analysis (Spring 2021)
Exam #1

Instructions: Please adhere to the following guidelines:

- Your responses to this exam are due by email at **1:00p on Friday, March 26**. I intend for this cutoff to be strict. You should not need anywhere near the full amount of time to complete the exam, but I am building in a generous cushion to allow for, e.g., technology issues. For your convenience—and to minimize the time and effort you need to spend on formatting—I have provided a template for your responses on which you should word-process your solutions and send to andrew.spieker@vumc.org by the deadline. Please label your solutions according to the format “LASTNAME-EXAM.docx.” I will confirm receipt of your exam. If you want to be cautious, you are welcome to e-mail exam drafts along the way (I will not start grading until after 1:00p on March 26, so there is no risk in sending drafts. Don’t worry about spamming my inbox; it won’t bother me at all—I’ll just grab the most recent copy at the deadline). I intend to score the exams, post the key, and provide detailed feedback to you by Monday, March 29.
 - There are five required problems (each with multiple sub-questions of varying length and difficulty) and two optional problems; there are five pages of appendix material. You are *not* expected to utilize software for any of these problems—all software output provided in this exam is sufficient to answer the questions.
 - Please read the instructions very carefully; answer no more and no less than what you are being asked to answer. You’ll notice throughout the exam that I repeatedly implore you to be concise. There are a lot of sub-questions on this exam, many of which should go relatively quickly and should only require very brief responses. My strong recommendation is to provide your responses to the problems you find easiest first, and then return to the more challenging ones.
 - This exam is open book/notes/calculator, but is an **individual effort**. You are not permitted to collaborate with individuals inside or outside the class, in-person, electronically, telepathically, or otherwise. You of course *may* consult any course materials including those on the course webpage. I cannot stop you from consulting other online resources, although doing so should not be necessary.
 - All questions regarding the exam should be directed to Andrew (andrew.spieker@vumc.org). If I am able to respond to your question, I will provide my response to the whole group (and I will of course anonymize your question). If I am unable to respond, I will let you know.
 - Upon completion of your exam, please indicate on the first page of the template whether you agree with the following statement: “On my honor, I have neither given nor received unauthorized aid on this exam.” If you have concerns about your ability to answer this in the affirmative, please turn in your exam anyway, and send me an email so we can discuss.
 - Please round any final calculations to a reasonable number of significant digits!
 - As is always the case in this class, any reference to logarithmic transformations are based on the *natural* logarithm (i.e., having base e).
 - **Importantly:** Take a deep breath — you’ve got this! This is an opportunity to showcase all of the hard work you’ve done so far this semester.
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1. 20 pts A study was conducted of $N = 975$ independently sampled children between ages 5 and 10 years with asthma. The study involved multiple goals, two of which we will discuss and explore in this problem.

The primary study objective was to investigate whether average time participating in physical activities (measured by average hours spent involved in physical activities per week over a six-week period; **physact**) varied across levels of asthma severity (measured by baseline forced expiratory volume; **fev**, in L). Consider the following simple linear regression model, used to address this goal:

$$\mathbf{E}[\text{physact}|\text{fev}] = \alpha_0 + \alpha_1 \text{fev} \quad (\text{Model 1})$$

One of the secondary study goals was to establish “normal ranges” of physical activity for children—that is, to formulate prediction intervals. To that end, consider the following simple linear regression model, which differs from that of Model 1 in that the predictor has undergone a log-transformation:

$$\mathbf{E}[\text{physact}|\text{fev}] = \beta_0 + \beta_1 \log(\text{fev}) \quad (\text{Model 2})$$

Stata output for Models 1 and 2 Are presented in Appendices I and II, respectively; each includes two diagnostic plots (a predictor-versus-residual plot and a normal quantile-quantile plot).

Parts (a) and (b) pertain specifically to the *primary* study objective.

- (a) State a literal interpretation for α_0 in plain language. To what degree is this interpretation meaningful in the real world?
- (b) State an interpretation for α_1 in plain language. Then,
 - i. State any assumptions necessary in order to estimate and conduct inference on α_1 in a way that is valid in large samples.
 - ii. Briefly discuss (maximum of three sentences) the extent to which the information provided in Appendix I demonstrates (or fails to demonstrate) evidence of violations to these assumptions.
 - iii. Briefly discuss (maximum of three sentences) the degree to which you believe the evidence of assumption violations you’ve noted in part (b) *severely* compromises your ability to address the study’s primary goal.

Parts (c) and (d) pertain specifically to the *secondary* study objective.

- (c) Compare the information provided in Appendices I and II; identify and briefly describe what information in these appendices makes it evident that Model 2 appears better equipped to accomplish the secondary goal as compared to Model 1.
- (d) Using the output from Model 2, form a prediction interval that would be estimated to encompass 95% of the distribution of the physical activity outcome among individuals with an FEV of 2.00.

Now, suppose that the study data also included information on each child’s age.

- (e) Briefly discuss (maximum of two sentences) *possible* advantages that could be gained in addressing the primary study objective from a model that *adjusts* for age.
-

2. 10 pts **Background:** One way in which vaccine candidates are screened in early stages of research is through comparisons of serologic immunogenicity markers (i.e., measures that pertain to identification of antibodies in the blood serum). The *antibody titer* is one such serologic measure, and is obtained by sequentially diluting a serum sample and testing each dilution for the antibody of interest; a participant's titer is defined to be the relative concentration of the *final* dilution that responds to an antibody test (higher titer values are indicative of a greater concentration of specific antibodies in the blood and are therefore more desirable). A vaccine is considered a good candidate if, after a certain period of time post-vaccination, subjects receiving the vaccine tend to have higher titers as compared to a control condition. Owing to the fact that titers are defined multiplicatively, it is standard to log-transform titer values and compare groups on the basis of the geometric mean titer.

A double-blind, placebo-controlled randomized phase-II trial of $N = 184$ subjects is conducted to evaluate the immunogenicity associated with a booster vaccine for protection against SARS-CoV-2, the virus responsible for COVID-19, among previously vaccinated subjects. In this study, the initial dilution of the original serum sample occurs at a ratio of 1:10, and the sample is diluted by a factor of two until response (or until a maximum of seven subsequent dilutions). Anyone whose serum does not respond to an antibody test at the initial concentration of 1:10 is given a titer value of 5, and anyone responding to a relative concentration of 1:1280 is given a titer value of 1280. Therefore, to be totally clear, the titer values in this study can take on the values 5, 10, 20, 40, 80, 160, 320, 640, and 1280. You may assume that titers are correlated within subjects over time. The variables collected in this study are provided below:

grp	treatment assignment (0 = control; 1 = SARS-CoV-2 candidate vaccine)
logpretiter	log-transformed pre-booster titer value
logtiter	log-transformed titer value three weeks following the booster

Consider the following two linear regression models, each of which you may freely assume to be correctly specified for the purposes of this problem.

$$\begin{aligned} \mathbf{E}[\text{logtiter}|\text{grp}] &= \beta_0^* + \beta_1^* \text{grp} && \text{(unadjusted)} \\ \mathbf{E}[\text{logtiter}|\text{grp}, \text{logpretiter}] &= \beta_0 + \beta_1 \text{grp} + \beta_2 \text{logpretiter} && \text{(adjusted)} \end{aligned}$$

-
- (a) Briefly justifying your response, what can you say about how the true values of the model parameters β_0^* and β_1^* relate to one another?
 - (b) If you had to choose only *one* of the above models to fit *a priori* (meaning, before actually conducting the analysis and having the opportunity to view the results), which would you choose? Briefly justify your response.
 - (c) In Appendix III, you are provided with Stata output for each of the above models. Based on your response to part (b), write a short (3-5 sentence) summary of the study results in the usual way that we have done in this class. Remember that for the purposes of this exam, it is totally legitimate to use homework keys and course notes as resources.
-

3. 20 pts This problem is a continuation of Problem 2. Titers suffer from inherent measurement error in the way they are derived. The easiest way to realize this is by example: take, for instance, someone whose serum *would* respond until a relative concentration of 1:159. Because of the sequential dilution procedure, that individual would be observed to have a titer value of 80 (because 1:80 reflects the maximum dilution *performed* at which the serum would be observed to respond), even though his or her *true* titer value is very clearly better reflected by 160. For better or for worse, clinical researchers have mostly responded to this dilemma by dichotomizing outcomes in one of several ways. One such way is to evaluate whether subjects have at least a four-fold rise in their post-booster titer from their pre-booster titer (this is typically referred to as *seroconversion*). For this problem, the variables under consideration are as follows:

grp	treatment assignment (0 = control; 1 = SARS-CoV-2 candidate vaccine)
logpretiter	log-transformed pre-booster titer value
seroconversion	indicator of at least four-fold rise in titer (0 = no; 1 = yes)

Consider the following two logistic regression models, each of which you may freely assume to be correctly specified for the purposes of this problem.

$$\begin{aligned} \text{logit}(P(\text{seroconversion} = 1|\text{grp})) &= \alpha_0^* + \alpha_1^* \text{grp} && \text{(unadjusted)} \\ \text{logit}(P(\text{seroconversion} = 1|\text{grp}, \text{logpretiter})) &= \alpha_0 + \alpha_1 \text{grp} + \alpha_2 \text{logpretiter} && \text{(adjusted)} \end{aligned}$$

-
- (a) If you had to choose only *one* of the two models above to fit *a priori* (meaning, before actually conducting the analysis and having the opportunity to view the results), which would you choose? Briefly justify your response.
- (b) In Appendix IV, you are provided with Stata output for each model. Based on your response to part (a), write a short (3-5 sentence) summary of the study results in the usual way that we have done in this class. Remember that for the purposes of this exam, it is totally legitimate to use homework keys and course notes as resources.
- (c) Regardless of your answers to parts (a)-(b), consider the 2×2 table below:

	Seroconversion	No seroconversion
Vaccine	<i>a</i>	<i>b</i>
Control	<i>c</i>	<i>d</i>

Despite the fact that you do not know the specific values of a , b , c , or d , use information provided in Appendix IV to state the value of the estimated odds ratio, $\overline{\text{OR}} = (a \times d)/(b \times c)$.

- (d) Regardless of your answers to parts (a)-(b), is it possible to use the information in Appendix IV to estimate the odds of seroconversion among control subjects with a pre-booster titer value of 80? If so, do so; if not, briefly explain why not.
- (e) Regardless of your answers to parts (a)-(b), is it possible to use the information in Appendix IV to estimate the probability of seroconversion among vaccine-candidate subjects with a pre-booster titer value of 160? If so, do so; if not, briefly explain why not.
- (f) Regardless of your answers to parts (a)-(b), is it possible to use the information in Appendix IV to determine a point estimate and 95% confidence interval for the the odds ratio that compares the odds of seroconversion between subgroups belonging to the same vaccination group but differing in their pre-booster titer value by a factor of two (or, to put it another way, by 100%)? If so, do so; if not, briefly explain why not.
-

4. 20 pts A case-control study was conducted among $N = 362$ prior or current smokers between the ages of 50 and 75 previously diagnosed with lung cancer to evaluate whether reducing or quitting smoking after diagnosis is associated with a lower odds of cancer recurrence. In particular, $n_0 = 180$ subjects were sampled whose cancer *did not* recur within a year after having been diagnosed and having gone into remission; $n_1 = 182$ subjects were sampled whose cancer *did* recur within a year after having been diagnosed and gone into remission. Enrolled subjects responded to a survey question regarding their smoking habits following cancer diagnosis. You may assume that in this study population, recurrence within a year is rare. The investigators of this study decided to adjust for age and allow an interaction between age and smoking status. The variables evaluated in this study are as follows:

rec	cancer recurrence within one year of remission (0 = no; 1 = yes)
smk	(0 = no change after diagnosis; 1 = reduced after diagnosis; 2 = quit after diagnosis)
age	age (years)

The investigators propose the following model:

$$\text{logit}(P(\text{rec}|\text{smk}, \text{age})) = \beta_0 + \beta_1 \text{age} + \beta_2 1(\text{smk}=1) + \beta_3 1(\text{smk}=2) + \beta_4 1(\text{smk}=1) \times \text{age} + \beta_5 1(\text{smk}=2) \times \text{age}.$$

The output for this model is presented in Appendix V, along with results of two hypothesis tests.

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- (a) Four scientific goals related to the study are listed below, and each could be addressed by testing some subset or combination of parameters of the above model (β_0 through β_5). For each of the four goals, first express a corresponding hypothesis test in terms of the model parameters. Then, examine the output provided in Appendix V; if you can use any of the provided output to summarize the statistical strength of evidence pertaining to the goal, do so (maximum: one sentence for each goal). If this cannot be done, simply say that not enough information is provided in Appendix V to learn about the result of the hypothesis test.
- i. **Goal A:** To evaluate whether there is evidence of an overall association between post-diagnosis change in smoking habits and odds of cancer recurrence.
 - ii. **Goal B:** To evaluate whether there is evidence that age modifies the association between change in smoking habits and odds of cancer recurrence.
 - iii. **Goal C:** To evaluate whether there is evidence of an association between age and odds of cancer recurrence among those reporting not changing their smoking habits after diagnosis.
 - iv. **Goal D:** To evaluate whether there is evidence of an association between age and odds of cancer recurrence among those reporting reducing their smoking habits after diagnosis.
- (b) Is it possible to use the information in Appendix V to estimate the odds of cancer recurrence among individuals 68 years old who had reported quitting smoking after diagnosis? If so, do so; if not, briefly explain why not.
- (c) Is it possible to use the information in Appendix V to obtain a point estimate and 95% confidence interval for the odds ratio comparing the odds of cancer recurrence between subgroups differing in age by *two years* and reporting not changing their smoking habits after diagnosis? If so, do so; if not, briefly explain why not.
- (d) Is it possible to use the information in Appendix V to approximate the risk ratio comparing the risk of cancer recurrence between subgroups differing in age by one year and reporting reducing smoking after diagnosis? If so, do so *and state what information allows you to do this*; if not, briefly explain why not.
-

5. 30 pts This question is about translating “biostatistics language” into concrete terms. For each sub-question, you are provided a variable description and a model, and are asked to use *plain language* to interpret: (i) a specific (possibly transformed) parameter, and (ii) a formal null hypothesis. You are *not* to include notation of regression models (e.g., $\mathbf{E}[Y|X = x]$); however, you *are* permitted to use numerals/percentages, or refer to variables that clarify subgroups (statements such as “among those with $X = 5$,” or “between subgroups differing in X by 10%” are acceptable). See the sample question/response below.

SAMPLE: Consider a linear regression model with binary (0/1) X and continuous Y :

$$\mathbf{E}[Y|X = x] = \beta_0 + \beta_1 x.$$

- i. Provide a plain-language interpretation for β_0 .

Ans: This is the mean value of Y among the subgroup defined by $X = 0$.

- ii. Provide a plain-language interpretation for the null hypothesis $H_0 : \beta_1 = 0$.

Ans: The null hypothesis is that the difference in mean Y between groups ($X = 0$ and $X = 1$) is zero.

- (a) Consider a linear regression model with continuous X , Z , and Y :

$$\mathbf{E}[Y|X = x, Z = z] = \beta_0 + \beta_1(x - \bar{x}) + \beta_2 z + \beta_3(x - \bar{x})z.$$

- i. Provide a plain-language interpretation for β_2 .

- ii. Provide a plain-language interpretation for the null hypothesis $H_0 : \beta_2 = \beta_3 = 0$.

- (b) Consider a logistic regression model with a continuous, positive-valued X and a binary (0/1) Y :

$$\text{logit}(\mathbf{P}(Y = 1|X = x)) = \beta_0 + \beta_1 \log(x).$$

- i. Provide a plain-language interpretation for $e^{\log(1.05)\beta_1} = 1.05^{\beta_1}$.

- ii. Provide a plain-language interpretation for the null hypothesis $H_0 : \beta_0 = 0$.

- (c) Consider a multinomial model with three-category values for both X and Y (0, 1, or 2).

$$\log\left(\frac{\mathbf{P}(Y = j|X = x)}{\mathbf{P}(Y = 0|X = x)}\right) = \beta_{0j} + \beta_{1j}1(x = 1) + \beta_{2j}1(x = 2), \quad j = 1, 2.$$

- i. Provide a plain-language interpretation for $e^{\beta_{12}}$.

- ii. Provide a plain-language interpretation for the null hypothesis $H_0 : \beta_{21} - \beta_{11} = 0$.

- (d) Consider a proportional odds model with a discrete, ordinal Y and continuous X , Z , and W :

$$\log\left(\frac{\mathbf{P}(Y \leq j|X = x, Z = z, W = w)}{\mathbf{P}(Y > j|X = x, Z = z, W = w)}\right) = \beta_{0j} - \beta_1 x - \beta_2 z - \beta_3 w - \beta_4 xz - \beta_5 xw - \beta_6 zw - \beta_7 xzw, \quad j = 0, 1.$$

- i. Provide a plain-language interpretation for e^{β_2} .

- ii. Provide a plain-language interpretation for the null hypothesis $H_0 : \beta_3 = \beta_5 = \beta_6 = \beta_7 = 0$.

- (e) Consider a Poisson model with non-negative discrete Y and binary (0/1) X and Z :

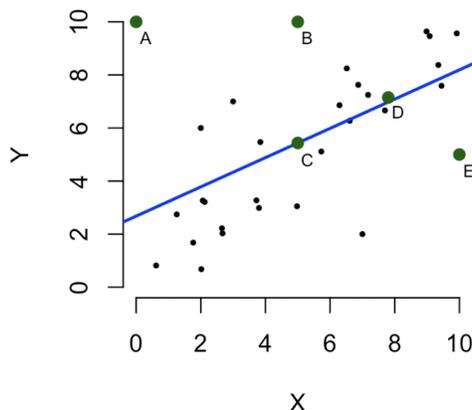
$$\log(\mathbf{E}[Y|X = x, Z = z]) = \beta_0 + \beta_1 x + \beta_2 z + \beta_3 xz.$$

- i. Provide a plain-language interpretation for e^{β_1} .

- ii. Provide a plain-language interpretation for the null hypothesis $H_0 : \beta_2 + \beta_3 = 0$.

6. **Optional problem 1:** This is an optional problem — I recommend not attempting it until you have completed and are satisfied with your answers to the required problems. A small amount of credit can be earned for attempting the problem, and an additional small amount of credit can be earned for a correct response.

Consider the following scatterplot of some variables X and Y , along with a line obtained from fitting an ordinary least squares linear regression model:



Each of the data points receives equal weight in the analysis, but I have labeled, shaded, and enlarged five points on the graph (A, B, C, D, and E) to bring them to your attention; the questions in this problem pertain to the five points in the figure. Here are some useful facts for the problem:

- Typically, the word *influence* implicitly refers to the parameter β_1 . When I refer to *influence* in this problem, I am doing so in accordance with this practice.
- The sample mean of X is 5.
- The estimated regression model parameters are $\widehat{\beta}_0 = 2.8$ and $\widehat{\beta}_1 = 0.54$.
- The emphasized points have coordinates A(0, 10); B(5, 10); C(5, ?); D(7.8, 7.2); E(10, 5). I deliberately left out the y -coordinate of point C.

Respond to each of the following parts, justifying each response in no more than a single sentence:

- Determine the sample mean of Y .
- State which two of the five points are best described as “high influence (on β_1) and high leverage.”
- State which of the five points is best described as “very low influence (on β_1) and modest leverage.”
- State which two of the five points are best described as “no influence (on β_1) and minimal leverage.”

7. **Optional problem 2:** This is an optional problem — I recommend not attempting it until you have completed and are satisfied with your answers to the required problems. A small amount of credit can be earned for attempting the problem, and an additional small amount of credit can be earned for a correct response.

Consider the following log-linear model (as per, for instance, Poisson regression):

$$\log(\mathbf{E}[Y|X = x]) = \beta_0 + \beta_1(x - \bar{x}) + \beta_2(x - \bar{x})^2.$$

State (in words, or mathematical notation) an interpretation for the value of $\beta_1 e^{\beta_0}$.

Hint: If you need a refresher about the in-class discussion on quadratic terms, see Slides 330 - 334 in Set 3 and/or refer back to the recording on February 23, about 20 minutes into the lecture. First try to tackle this problem in the un-centered case, following the process we used to handle interpretation of β_1 in a linear regression model with a quadratic term—this requires a small amount of differential calculus, like in the course notes. If you took calculus but have forgotten some of the differentiation rules, I will provide you with all the ones you'll need below. If you do not want to do the calculus, you're welcome to just take a guess! :)

$$\frac{d}{dx} c \times x = c.$$

$$\frac{d}{dx} x^p = px^{p-1}.$$

$$\frac{d}{dx} e^x = e^x.$$

$$\frac{d}{dx} f(g(x)) = f'(g(x))g'(x).$$

$$\frac{d}{dx} f(x - x_0) \Big|_{x=x_0} = \frac{d}{dx} f(x) \Big|_{x=0}.$$

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Appendix Material for Exam 1

APPENDIX I: Stata output for Problem 1

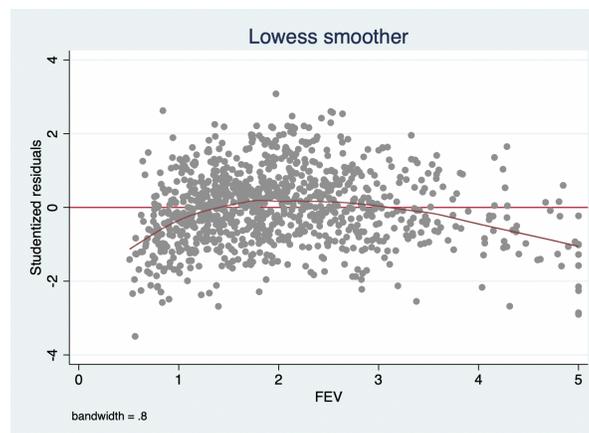
*** ANALYSIS OF UNTRANSFORMED FEV ***

```
. regress physact fev, robust
```

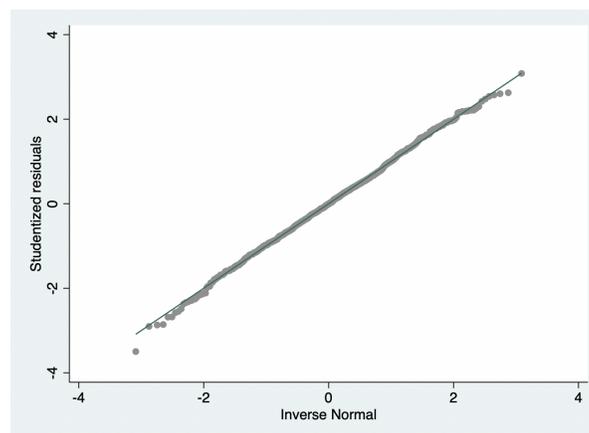
```
Linear regression                Number of obs   =       975
                                F(1, 973)      =       500.42
                                Prob > F           =       0.0000
                                R-squared          =       0.3869
                                Root MSE       =       .41126
```

physact	Coef.	Robust Std. Err.	t	P> t	[95% Conf. Interval]
fev	.4956053	.0173399	28.58	0.000	.4615774 .5296331
_cons	1.65395	.0366488	45.13	0.000	1.58203 1.72587

Diagnostic Plot #1: Predictor vs. studentized residuals.



Diagnostic Plot #2: Quantile-quantile plot.



APPENDIX II: Stata output for Problem 1 (continued)

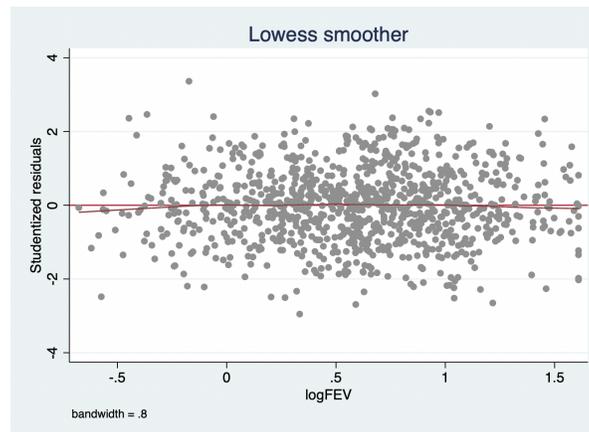
*** ANALYSIS OF LOG-TRANSFORMED FEV ***

```
. regress physact logfev, robust
```

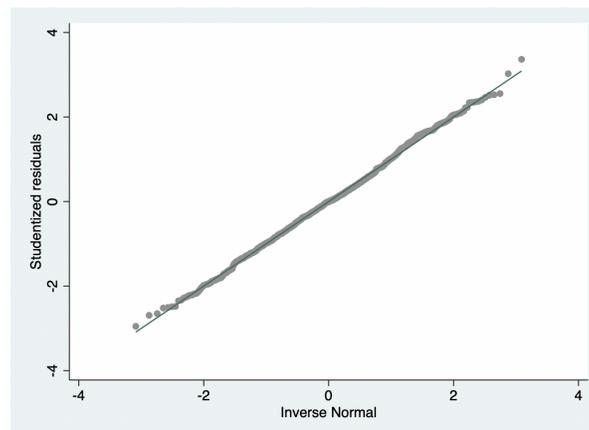
```
Linear regression                Number of obs   =       975
                                F(1, 973)      =       679.16
                                Prob > F            =       0.0000
                                R-squared           =       0.4145
                                Root MSE        =       .40189
```

physact	Coef.	Robust Std. Err.	t	P> t	[95% Conf. Interval]
logfev	1.041884	.0280954	37.08	0.000	.9867493 1.097018
_cons	2.031183	.0206557	98.34	0.000	1.990648 2.071718

Diagnostic Plot #1: Predictor vs. studentized residuals.



Diagnostic Plot #2: Quantile-quantile plot.



APPENDIX III: Stata output for Problem 2

*** UNADJUSTED ANALYSIS ***

. regress logtiter grp, robust

```

Linear regression                Number of obs   =       184
                                F(1, 182)      =        3.03
                                Prob > F           =       0.0832
                                R-squared          =       0.0164
                                Root MSE        =       .99738
  
```

		Coef.	Robust Std. Err.	t	P> t	[95% Conf. Interval]	
logtiter							
grp		.2561631	.1470555	1.74	0.083	-.0339898	.546316
_cons		4.020385	.1035813	38.81	0.000	3.81601	4.224759

*** ADJUSTED ANALYSIS ***

. regress logtiter grp logpretiter, robust

```

Linear regression                Number of obs   =       184
                                F(2, 181)      =       75.84
                                Prob > F           =       0.0000
                                R-squared          =       0.4564
                                Root MSE        =       .74352
  
```

		Coef.	Robust Std. Err.	t	P> t	[95% Conf. Interval]	
logtiter							
grp		.2253742	.109487	2.06	0.041	.0093392	.4414092
logpretiter		.4540608	.0371566	12.22	0.000	.380745	.5273766
_cons		2.249621	.1670856	13.46	0.000	1.919935	2.579307

APPENDIX IV: Stata output for Problem 3

*** UNADJUSTED ANALYSIS ***

. logit seroconversion grp, robust nolog

```
Logistic regression                Number of obs   =       184
                                   Wald chi2(1)      =         0.26
                                   Prob > chi2       =         0.6081
Log pseudolikelihood = -102.22404   Pseudo R2      =         0.0013
```

seroconversion		Coef.	Robust Std. Err.	z	P> z	[95% Conf. Interval]	
grp		.1767036	.3445596	0.51	0.608	-.4986209	.852028
_cons		-1.218157	.2490798	-4.89	0.000	-1.706345	-.7299701

*** ADJUSTED ANALYSIS ***

. logit seroconversion grp logpt, robust nolog

```
Logistic regression                Number of obs   =       184
                                   Wald chi2(2)      =        34.83
                                   Prob > chi2       =         0.0000
Log pseudolikelihood = -56.502458   Pseudo R2      =         0.3472
```

seroconversion		Coef.	Robust Std. Err.	z	P> z	[95% Conf. Interval]	
grp		.677033	.4843872	1.40	0.162	-.2723485	1.626415
logpt		1.511318	.2570426	5.88	0.000	1.007523	2.015112
_cons		-3.577783	.7648304	-4.68	0.000	-5.076823	-2.078743

APPENDIX V: Stata output for Problem 4

```
. logit rec c.age##i.smk, robust nolog
```

```
Logistic regression                Number of obs   =       362
                                Wald chi2(5)     =         7.30
                                Prob > chi2          =         0.1995
Log pseudolikelihood = -151.05378   Pseudo R2      =         0.0313
```

rec	Coef.	Robust Std. Err.	z	P> z	[95% Conf. Interval]	
age	.0685194	.0498011	1.38	0.169	-.0290891	.1661278
smk						
1	2.805594	4.604232	0.61	0.542	-6.218536	11.82972
2	-7.793166	8.879124	-0.88	0.380	-25.19593	9.609596
smk#c.age						
1	-.0403019	.0585656	-0.69	0.491	-.1550883	.0744846
2	.106017	.1199353	0.88	0.377	-.1290519	.3410858
_cons	-3.536572	3.934267	-0.90	0.369	-11.24759	4.17445

```
. lincom age + 1.smk#c.age
```

```
( 1) [rec]age + [rec]1.smk#c.age = 0
```

rec	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
(1)	.0282175	.0308184	0.92	0.360	-.0321855	.0886205

```
. testparm smk#c.age
```

```
( 1) [rec]1.smk#c.age = 0
```

```
( 2) [rec]2.smk#c.age = 0
```

```
      chi2( 2) =      1.92
      Prob > chi2 =      0.3820
```